



丘成桐数学科学中心
YAU MATHEMATICAL SCIENCES CENTER



希尔伯特模和多变量算子理论

Multivariable Operator Theory-A Hilbert Module Approach

December 8-12, 2025

Room A-103, TSIMF

组织者 ORGANIZERS

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Yi Wang(王奕), Chongqing University

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About the conference

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Multivariable Operator Theory - A Hilbert Module Approach

Date

December 8-12, 2025

Venue

Room A-103, TSIMF

Organizers

Gadadhar Misra, Indian Statistical Institute

Jaydeb Sarkar, Indian Statistical Institute

Kai Wang (王凯), Fudan University

Yi Wang (王奕), Chongqing University

Abstract

The topic of this workshop is the Hilbert module approach in operator theory, with an emphasis on the techniques of analytic function theory, complex geometry, and algebraic geometry. Operator theory, and more specifically, multivariable operator theory, and the aforementioned subjects share intimate connections. These subjects are closely related to a variety of disciplines, including PDE, operator algebras, linear analysis, and harmonic analysis, to mention only a few. The theory of operators evolved from the study of normal operators, Toeplitz operators, the Volterra operator, and index theory. A milestone is the Nagy-Foias analytic operator model theory developed in the 1950s and 60s, which states that every bounded linear operator can be represented as a compression of the shift operator to a certain Hilbert space of holomorphic functions. This fact reaffirms the algebraic link between traditional operator theory and function theory. Around the same time, index theory was given a topological, geometrical, and analytic framework in the deep work of Brown-Douglas-Fillmore, which in part motivated the development of noncommutative geometry. In light of these and other intriguing theories, it became clear that a more general framework is required to unify all the pertinent concepts. R. G. Douglas' introduction of Hilbert modules in the 1980s came at an opportune time. The theory makes available diverse tools and techniques from a wide range of fields, such as commutative algebra, complex geometry, several complex variables, and algebraic geometry, to name a few, for the study of operator systems and multivariable spectral theory. Indeed, with the passage of time, a great number of achievements have been made along this line, for example in the study of

- 1) Cowen-Douglas operators,
- 2) distinguished varieties (a concept introduced by Rudin),
- 3) the interpolation problem,
- 4) extension of analytic functions from algebraic variety,
- 5) bounded symmetric domains,
- 6) the Chevalley-Shephard-Todd theorem,
- 7) the Riemann zeta function in terms of infinite polydisc,

8) characteristic spaces.

Additional success has been recorded in the study of Samuel multiplicity, analytic K-homology, projective spectrum, bounded analytic functions, etc.

The theory of Hilbert modules has been very actively pursued since the last meeting on this subject, which took place at TSIMF shortly before the Covid pandemic. This proposed workshop aims to analyze the subject's evolution in recent years and outline possible future directions for growth. Particular attention will be given to early-career researchers. Indeed, a significant percent of the proposed participants are PhD students, postdocs, and tenure-track assistant professors. The proposed workshop will provide a good opportunity for them to communicate in-person and foster collaborations.

Description of the aim

The primary aim of the workshop is to provide a platform for the dissemination of recent research discoveries and to highlight the key challenges in the field of operator theory after reformulating them in the language of Hilbert modules. Over the past three decades, it has been amply clear that this reformulation is not merely a choice of language. It in fact creates a new landscape. For instance, submodules in several variable have complicated structure, and classifications of them become an appealing and yet rather challenging task. On the other hand, the study of quotient modules amounts to develop a multivariable Nagy-Foias model theory, which provides a fertile ground for the growth of multivariable operator theory.

The main themes of this workshop are as follows:

- (A) Submodules and quotient modules over function algebras and the corresponding resolutions of Hilbert modules.
- (B) Function theory on an infinite polydisc.
- (C) The theory of bounded analytic functions in several variables and its connection to Hilbert modules.
- (D) Multivariable spectral theory.

In terms of scientific goals, it is understood that function theory, multivariable operator theory, and the Hilbert module structure that goes with them depend heavily on the specific domain. The function theory of the open unit ball and that of the open unit polydisc, for example, differ significantly. Another emerging theory, as far as domain-related studies are concerned, is the Riemann zeta function in terms of function theory on an infinite polydisc. Indeed, the manner in which function theories vary across distinct domains is remarkable and fascinating. How these differences play a role in the study of Hilbert modules is worth serious investigation. It is undoubtedly a part of the allure of Hilbert modules and multivariable operator theory.

Another important subject concerns with essentially normal quotient modules. On infinite-dimensional Hilbert spaces, compact operators are the "small" objects that introduce numerical invariants, such as the index of a Fredholm operator. Self commutators $[T, T^*]$ and cross commutators $[T_1, T_2^*]$ of multiplication operators T, T_1 , and T_2 on Hilbert modules are often "small", prompting the question whether they are in fact "smaller", i.e., whether they belong to the so-called Schatten p -class. For homogeneous submodules in the Drury-Arveson space over the unit ball, this question is framed as the Arveson-Douglas conjecture, which has been a tantalizing open problem for some time. In fact, it is anticipated that the answer depends on the geometry of the zero

variety of such submodules. This connection facilitates the study of analytic K-homology in an appropriate way. This workshop shall review the current status of the conjecture and investigate on recent novel approaches.

In addition to the aforementioned topics, the workshop also concerns with the following list of problems.

- (i) The classification of submodules and quotient modules of analytic Hilbert modules.
- (ii) Analytic and algebraic invariants of the submodules and quotient modules with respect to unitary equivalence, similarity, and quasi-similarity.
- (iii) Investigating the essential normality of Hilbert modules, including the Douglas-Arveson conjecture mentioned above.
- (iv) The problem of holomorphic imprimitivities as the restrictions of imprimitivities in the sense of Mackey and its close connection with the subnormality of Cowen-Douglas modules.
- (v) The problem of finding a complete set of invariants for holomorphic hermitian sheaves.
- (vi) Interpolation on various domains and its consequences for Hilbert modules.
- (vii) Spectral theory in the setting of Hilbert modules.
- (viii) Beurling-Wintner dilation problem.
- (ix) Szego's problem in infinite polydisc.
- (x) Determinantal point process from multivariable operator theory. Undoubtedly, some of the aforementioned problems are complex and necessitate a long-term approach. We hope that this workshop will also help identify rising stars who might lead future efforts in addressing these challenges. Therefore, it will be in our best interest to invite a large number of young researchers to this workshop and foster their growth for the advancement of mathematics.

Previous Workshops: Some of the events that have taken place in the past few 15 years:

- (i) Hilbert Modules in Analytic Function Spaces workshop, Tsinghua Sanya International Mathematics Forum (TSIMF), Sanya, China, Dec 30, 2019 - Jan 3, 2020.
- (ii) Hilbert Modules in Analytic Function Spaces workshop, Tsinghua Sanya International Mathematics Forum (TISMF), Sanya, China, May 22-26, 2017.
- (iii) Multivariate Operator Theory, BIRS, Banff, Canada, April 6 - 10, 2015.
- (iv) Hilbert Modules and Complex Geometry, Oberwolfach, Germany, Apr 20- 26, 2014.
- (v) Multivariate Operator Theory, BIRS, Banff, Canada, August 15 - 20, 2010.
- (vi) Hilbert Modules and Complex Geometry, Oberwolfach, Germany, Apr 12- 18, 2009.

Schedule

Time&Date	Monday (December 8)	Tuesday (December 9)	Wednesday (December 10)	Thursday (December 11)	Friday (December 12)
7:30~8:30	Breakfast (60 minutes)				
Chair	Gadadhar Misra	Yi Wang	Harald Upmeyer	Junyun Hu	Dan Timotin
8:40-8:45	Opening				
8:45-9:30	Harald Upmeyer	Michael Hartz	Dan Timotin	Orr Shalit	Jiayang Yu
9:35-10:20	Shuaibing Luo	Kui Ji	Pan Ma	Lijia Ding	James Pascoe
10:20-10:50	Coffee Break (30 minutes)				
Chair	Jingbo Xia	Xiang Tang	Xianmin Xu	Yongjiang Duan	Shuaibing Luo
10:50-11:35	Soumitra Ghara	Zipeng Wang	Deepak Pradhan	Xiangdi Fu	Penghui Wang
11:40-12:25	Fugang Yan	Yongjiang Duan	Jingbo Xia	Kelly Bickel	Paramita Pramanick
12:30-13:30	Lunch (60 minutes)				
Chair	Yan Wu	Li Chen	Free Discussion	Maofa Wang	Kui Ji
14:00-14:45	Siyu Wang	Lukasz Kosinski		Guanlong Bao	Constanze Liaw
14:45-15:20	Coffee Break	Group Photo		Coffee Break (30 minutes)	
15:20-16:05	Hansong Huang	Surjit Kumar		Victor Bailey	Chao Zu
16:10-16:55	Zbigniew Burdak	Maofa Wang		Sameer Chavan	Yixin Yang
18:00-19:30	Dinner	Banquet 18:00-20:00	Dinner (90 minutes)		

Note: Each talk will last 45 minutes, with an additional 5 minutes for Q&A.

December 8, 2025 - Monday

Time	Name	Title
7:30~8:30	Breakfast (60 minutes)	
Chair	Gadadhar Misra	
8:40-8:45	Opening	
8:45-9:30	Harald Upmeyer	A New Type of Hilbert Modules
9:35-10:20	Shuaibing Luo	Doubly commuting invariant subspaces of $L^2(\mathbb{T}^n)$
10:20-10:50	Coffee Break (30 minutes)	
Chair	Jingbo Xia	
10:50-11:35	Soumitra Ghara	Commuting tuple of multiplication operators homogeneous under the unitary group
11:40-12:25	Fugang Yan	Toeplitz operators and α -Berezin transforms on the Bergman space
12:30-13:30	Lunch (60 minutes)	
Chair	Yan Wu	
14:00-14:45	Siyu Wang	Fractional derivatives on Bloch and Bergman spaces
14:45-15:20	Coffee Break (30 minutes)	
15:20-16:05	Hansong Huang	Critical points, finite Blaschke products and Riemann surface: on multiplication operators over the Bergman space
16:10-16:55	Zbigniew Burdak	Pairs of compatible isometries - model, spectrum and applications
18:00-19:30	Dinner (90 minutes)	

December 9, 2025 - Tuesday

Time	Name	Title
7:30~8:30	Breakfast (60 minutes)	
Chair	Yi Wang	
8:45-9:30	Michael Hartz	von Neumann's inequality on the polydisc
9:35-10:20	Kui Ji	On the classification of \mathcal{J} -holomorphic curves
10:20-10:50	Coffee Break (30 minutes)	
Chair	Xiang Tang	
10:50-11:35	Zipeng Wang	The Fourier decay of cascade measures
11:40-12:25	Yongjiang Duan	Carelsen Embedding for doubling weighted Bergman-Orlicz spaces and its applications
12:30-13:30	Lunch (60 minutes)	
Chair	Li Chen	
14:00-14:45	Lukasz Kosinski	Converse to Lempert's theorem and extension sets
14:45-15:20	Coffee Break (30 minutes)&Group Photo	
15:20-16:05	Surjit Kumar	On weakly $\mathcal{U}(d)$ -homogeneous Tuple of Operators
16:10-16:55	Maofa Wang	Commutants of composition operators on Fock space
Banquet 18:00-20:00		

December 10, 2025 - Wednesday

Time	Name	Title
7:30~8:30	Breakfast (60 minutes)	
Chair	Harald Upmeyer	
8:45-9:30	Dan Timotin	Characteristic functions and invariant subspaces: old and new
9:35-10:20	Pan Ma	Cubic matrix Szegő equation and Hankel operators
10:20-10:50	Coffee Break (30 minutes)	
Chair	Xianmin Xu	
10:50-11:35	Deepak Pradhan	Inner and characteristic functions in polydisks
11:40-12:25	Jingbo Xia	Boyd indices and the complete story of the Berger-Coburn phenomenon
12:30-13:30	Lunch (60 minutes)	
14:00-14:45	Free Discussion	
14:45-15:20		
15:20-16:05		
16:10-16:55		
18:00-19:30	Dinner (90 minutes)	

December 11, 2025 - Thursday

Time	Name	Title
7:30~8:30	Breakfast (60 minutes)	
Chair	Junyun Hu	
8:45-9:30	Orr Shalit	A joint spectral radius for tuples of operators
9:35-10:20	Lijia Ding	Helton-Howe trace formulae on quotient modules
10:20-10:50	Coffee Break (30 minutes)	
Chair	Yongjiang Duan	
10:50-11:35	Xiangdi Fu	Extension of contractive projections
11:40-12:25	Kelly Bickel	Some Clark Theory on the Bidisk
12:30-13:30	Lunch (60 minutes)	
Chair	Maofa Wang	
14:00-14:45	Guanlong Bao	Some results on analytic function spaces by potentials
14:45-15:20	Coffee Break (30 minutes)	
15:20-16:05	Victor Bailey	Dynamical Frames and Hyperinvariant Subspaces
16:10-16:55	Sameer Chavan	Subnormality of Brownian-type operators
18:00-19:30	Dinner (90 minutes)	

December 12, 2025 - Friday

Time	Name	Title
7:30~8:30	Breakfast (60 minutes)	
Chair	Dan Timotin	
8:45-9:30	Jiayang Yu	Measures on General Co-dimensional Surfaces in Infinite Dimensions and Stokes Type Theorems
9:35-10:20	James Pascoe	Constrained sphere packing and the interpolation problem for positive definite functions
10:20-10:50	Coffee Break (30 minutes)	
Chair	Shuaibing Luo	
10:50-11:35	Penghui Wang	Essential normality of quotient modules vs Hilbert-Schmidtness of submodules in Hardy modules over the polydisc
11:40-12:25	Paramita Pramanick	Brown-Halmos Characterization, and Function Theory on the Tetrablock
12:30-13:30	Lunch (60 minutes)	
Chair	Kui Ji	
14:00-14:45	Constanze Liaw	Singular Spectrum under a Wide Class of Perturbations
14:45-15:20	Coffee Break (30 minutes)	
15:20-16:05	Chao Zu	Hilbert-Schmidt norm estimates of homogeneous polynomial submodules in Hardy space over the bidisk
16:10-16:55	Yixin Yang	The complete Nevanlinna-Pick property for sub-Hardy/Bergman space
18:00-19:30	Dinner (90 minutes)	



Titles and Abstracts

A New Type of Hilbert Modules

Harald Upmeyer

University of Marburg, Germany

Classically, Hilbert modules are considered for (multivariable) holomorphic functions. In this talk we introduce a new type of Hilbert modules which do not consist of holomorphic functions but instead involve Dolbeault cohomology classes of differential forms of higher degree. We give examples from representation theory (discrete series of semi-simple Lie groups) which show that the holomorphic case gives only a small fraction of the theory, whereas the cohomology approach yields a much more complete picture. We also show that many fundamental problems studied in the holomorphic case can also be addressed for this new type of Hilbert modules. An interesting feature of the new approach is that it is already non-trivial in the strongly pseudo-convex case of the unit ball. This will be explained in detail in the lecture.

Doubly commuting invariant subspaces of $L^2(\mathbb{T}^n)$

Shuaibing Luo (罗率兵)

Hunan University, China

In this talk, we discuss the invariant subspace M for the tuple of multiplication operators $M_z = (M_{z_1}, \dots, M_{z_n})$ on $L^2(\mathbb{T}^n)$ under the condition that the restricted tuple $M_z|_M = (M_{z_1}|_M, \dots, M_{z_n}|_M)$ is doubly commuting. We also formulate our invariant subspace theorem using intersecting families of subsets of $\{1, 2, \dots, n\}$. As applications of our result, we obtain invariant subspace theorems for tuple of shift related operators including Beurling type theorems on the Hardy space of the polydisk.

Commuting tuple of multiplication operators homogeneous under the unitary group

Soumitra Ghara

IIT Kharagpur, India

Let $\mathcal{U}(d)$ be the group of $d \times d$ unitary matrices. In this talk, we will discuss conditions to ensure that a $\mathcal{U}(d)$ -homogeneous d -tuple \mathbf{T} is unitarily equivalent to the operator of multiplication by the coordinate functions on some reproducing kernel Hilbert space $\mathcal{H}_K(\mathbb{B}_d, \mathbb{C}^n) \subseteq \text{Hol}(\mathbb{B}_d, \mathbb{C}^n)$, $n = \dim \bigcap_{j=1}^d \ker T_j^*$. We will describe this class of $\mathcal{U}(d)$ -homogeneous operators, equivalently, non-negative kernels K quasi-invariant under the action of $\mathcal{U}(d)$. We will also present a classification of quasi-invariant kernels K transforming under $\mathcal{U}(d)$ with two specific choice of multipliers. An explicit criterion for boundedness, reducibility and mutual unitary equivalence among these operators will also be discussed. This is a joint work with S. Kumar, G. Misra and P. Pramanick.

Toeplitz operators and α -Berezin transforms on the Bergman space

Fugang Yan(晏福刚)
Chongqing University, China

The characterization of bounded Toeplitz operators with integrable symbols in the Bergman space is an open problem even in the simplest case of the unweighted Bergman space of unit disc. In this talk, we will introduce the recent progresses related to this problem. In particular, we study this problem via α -Berezin transforms. We show that if a Toeplitz operator T_f with $f \in L^2(\mathbb{D})$ is bounded, then α -Berezin transform of f is bounded for all $\alpha > -1/2$. We also show that for $-1 < \alpha < 1$, the boundedness for the α -Berezin transform of f cannot imply the boundedness of the Toeplitz operator T_f . This talk is based on a joint work with professor Dechao Zheng.

Fractional derivatives on Bloch and Bergman spaces

Siyu Wang(王司宇)
Fudan University, China

In this talk, we will show that the classical Bloch space and the Bergman space A_{η}^p , induced by a radial doubling weight η , can be characterized by using the fractional derivative

$$f \mapsto R_{\nu, \omega}(f)(z) = \sum_{k=0}^{\infty} \frac{\nu_{2k+1}}{\omega_{2k+1}} \widehat{f}(k) z^k, \quad z \in \mathbb{D},$$

induced by two radial weights admitting certain doubling conditions. Here

$$\omega_{2k+1} = \int_0^1 r^{2k+1} \omega(r) dr$$

are the odd moments of ω , and $\widehat{f}(k)$ stands for the Maclaurin coefficient of the analytic function f in the unit disc \mathbb{D} .

The arguments employed here rely on the natural integral representation

$$R_{\nu, \omega}(f)(z) = \int_{\mathbb{D}} f(\zeta) \overline{B_z^{\omega}(\zeta)} \nu(\zeta) dA(\zeta), \quad z \in \mathbb{D}, \quad f \in L_{\nu}^1$$

via the Bergman reproducing kernels B_z^{ω} of the Hilbert space A_{ω}^2 . On the path to our main result, we also study the boundedness of fractional derivative $R_{\nu, \omega}$ as an integral operator from weighted L^{∞} to weighted Bloch spaces. This talk is based on a joint work with A. Perälä and J. Rättyä.

Critical points, finite Blaschke products and Riemann surface: on multiplication operators over the Bergman space

Hansong Huang(黄寒松)

East China University of Science and Technology, China

In this talk, we first review recent advances in characterizing the reducing subspaces of multiplication operators induced by several classes of inner functions on the Bergman space $L_a^2(\mathbb{D})$ over the unit disk. Specifically, for a finite Blaschke product B , it is known that the von Neumann algebra $\mathcal{V}^*(B) = \{M_B, M_B^*\}'$ is abelian, where M_B is the multiplication operator defined by B on the Bergman space $L_a^2(\mathbb{D})$. It was proven that the number of minimal projections in $\mathcal{V}^*(B)$ is equal to that of components of the Riemann surface \mathcal{S}_B contained in \mathbb{D}^2 . However, determining this integer for a specific finite Blaschke product B is a challenging task. We take an approach by analyzing the analytic continuations and identifying its critical points. This approach reveals an interplay between function theory, operator theory, and complex geometry.

This is a joint work with Danni Guo, Shan Li, Shuaibing Luo.

Pairs of compatible isometries - model, spectrum and applications

Zbigniew Burdak

University of Agriculture in Krakow, Poland

Pair of isometries is called compatible if projections on powers of range spaces commute for any pair of powers. In the talk we recall the model, show an application to stochastic processes and calculate Taylor spectrum in some cases. The application describes evanescent part for weakly stationary stochastic process with a half-plane past. Taylor spectrum in the case of pairs given by diagrams (which is one of the types in the model) is a proper subset of a bi-disk and may be of any measure in $(0, \pi^2)$.

von Neumann's inequality on the polydisc

Michael Hartz

Saarland University, Germany

The Schur-Agler norm of a d -variable polynomial p is defined as

$$\|p\|_{SA} = \sup \{ \|p(T_1, \dots, T_d)\| : T_1, \dots, T_d \text{ commuting contractions on Hilbert space} \}.$$

Classical results of von Neumann and Andô show that if $d = 1$ and $d = 2$, then the Schur-Agler norm equals the supremum norm on \mathbb{D}^d . If $d \geq 3$, this is no longer true, but it is still now known whether the Schur-Agler norm is equivalent to the supremum norm.

I will talk about new upper and lower bounds for the Schur-Agler norm of homogeneous polynomials in $d \geq 3$ variables. This partly joint work with Dexie Lin and Yi Wang.

On the classification of \mathcal{J} -holomorphic curves

Kui Ji(纪奎)

Hebei Normal University, China

Let \mathcal{H} be a complex separable Hilbert space. For Ω an open connected subset of \mathbb{C} , we shall say that a map $f : \Omega \rightarrow \text{Gr}(n, \mathcal{H})$ is a holomorphic curve, if there exist n holomorphic \mathcal{H} -valued functions $\gamma_1, \gamma_2, \dots, \gamma_n$ on Ω such that

$$f(w) = \bigvee \{ \gamma_1(w), \gamma_2(w), \dots, \gamma_n(w) \}, w \in \Omega,$$

where $\text{Gr}(n, \mathcal{H})$ denotes the Grassmann manifold, the set of all n -dimensional subspaces of \mathcal{H} . The homogeneous curves, weakly homogeneous curves in Cowen-Douglas class are introduced A. Koranyi and G. Misra. The relevant researches on this type of curves has established the relationship between group representation theory, operator theory, Hilbert module and complex geometry.

In this talk, we will introduce a new and large class of holomorphic curves named as \mathcal{J} -holomorphic curves which including homogeneous curves, weakly homogeneous curves. By using some geometric invariants, we also give a similarity classification theorem of this kind curves.

The Fourier decay of cascade measures

Zipeng Wang(王子鹏)

Chongqing University, China

I will report our solutions to the Mandelbrot problem/conjecture (1974) and the Kahane problem (1993), which concern the optimal Fourier decay of cascade measures originally motivated by the K41 turbulence model.

This report requires no prior knowledge of probability theory and is particularly well-suited for experts and scholars with a background in functional analysis.

This is a series of joint works with Xinxin Chen, Yong Han, and Yanqi Qiu.

Carelsen Embedding for doubling weighted Bergman-Orlicz spaces and its applications

Yongjiang Duan(段永江)

Jinan University, China

We provide geometric characterizations for the positive Borel measures μ such that the weighted Bergman-Orlicz space $A_{\omega}^{\Phi_1}$ is continuously embedded into $L_{\mu}^{\Phi_2}$, where Φ_1, Φ_2 are Young functions satisfying certain growth conditions, and the radial weight ω on the unit disk satisfies the doubling condition. As applications, we give the characterizations of the Toeplitz operators, Volterra operators and composition operators between the doubling weighted Bergman-Orlicz spaces. This is joint with Min Dong, Kunyu Guo and Siyu Wang.

Converse to Lempert's theorem and extension sets

Lukasz Kosinski
Jagiellonian University, Poland

We will recall Lempert's theorem, explain how it arises in Several Complex Variables, and describe its connections with Operator Theory. We will then discuss the extent to which it works and how a converse arises in the context of the Extension Property. The talk is based on joint work with J. E. McCarthy and J. Agler.

On weakly $\mathcal{U}(d)$ -homogeneous Tuple of Operators

Surjit Kumar
IIT Madras, India

The unitary group $\mathcal{U}(d)$ acts naturally on any d -tuple $\mathbf{T} = (T_1, \dots, T_d)$ of commuting bounded linear operators on a complex separable Hilbert space \mathcal{H} . A commuting d -tuple $T = (T_1, \dots, T_d)$ is called weakly $\mathcal{U}(d)$ -homogeneous if, for every $u \in \mathcal{U}(d)$, there exists a bounded invertible operator $\Gamma(u)$ on \mathcal{H} such that

$$\Gamma(u)T_j = (u \cdot T)_j\Gamma(u), \quad j = 1, \dots, d.$$

Every $\mathcal{U}(d)$ -homogeneous tuple is clearly weakly $\mathcal{U}(d)$ -homogeneous. Furthermore, any commuting d -tuple that is similar to a $\mathcal{U}(d)$ -homogeneous tuple must be weakly $\mathcal{U}(d)$ homogeneous. In this talk, we identify a few classes of weakly $\mathcal{U}(d)$ -homogeneous operator tuples that are, in fact, similar to $\mathcal{U}(d)$ -homogeneous tuples. One such class is the family of d -variable weighted shifts. In this class, a spherical isometry is weakly $\mathcal{U}(d)$ -homogeneous if and only if it is similar to the Szegő shift.

This is a joint work with Soumitra Ghara, and Shailesh Trivedi.

Commutants of composition operators on Fock space

Maofa Wang(王茂发)
Wuhan University, China

This talk will give some profound and comprehensive characterizations on commutants of composition operators on Fock space of several variables. Also we consider the asymptotic behaviour of discrete or continuous semigroups of such operators. This is joint work with Frédéric Bayart and Xingxing Yao.

Characteristic functions and invariant subspaces: old and new

Dan Timotin

Simion Stoilow Institute of Mathematics of the Romanian Academy, Romania

In the Sz.Nagy-Foias theory of contractions on a Hilbert spaces, an important point is the identification of a one-to-one correspondence between the invariant subspaces of the contraction and certain factorizations of its characteristic function. We will discuss this correspondence, including details on its history. Subsequently we will present some recent applications and extensions, in view also of possible generalizations.

Cubic matrix Szegő equation and Hankel operators

Pan Ma(马攀)

Central South University, China

In this talk, we will present some progress on the flow of cubic matrix Szegő equation on the unit circle \mathbb{T} which is the evolution equation on $H^2(\mathbb{T}, \mathbb{C}^{m \times n})$

$$i\partial_t U = \mathbb{P}(UU^*U), U = U(t, x) \in \mathbb{C}^{m \times n}, (t, x) \in \mathbb{R} \times \mathbb{T},$$

where \mathbb{P} denotes the matrix Szegő projection from $L^2(\mathbb{T}, \mathbb{C}^{m \times n})$ onto $H^2(\mathbb{T}, \mathbb{C}^{m \times n})$.

Inner and characteristic functions in polydiscs

Deepak Kumar Pradhan

IIT Hyderabad, India

A d -tuple of contractions $\mathbf{T} \in \mathcal{B}(\mathcal{H})^d$ is said to be a pure Szegő tuple if $\prod_{i=1}^d (I - T_i T_i^*) \geq 0$ and $T_i^{*n} \xrightarrow{SOT} 0$. Further, a pure Szegő tuple \mathbf{T} , is said to be of Beurling type if the model space of \mathbf{T} is a Beurling quotient module in the Hardy space of polydisc. In this talk, we will define the operator-valued characteristic function $\Theta_{\mathbf{T}}(z)$ on the polydisc \mathbb{D}^n for pure Szegő tuple \mathbf{T} of Beurling type. We also show that $\Theta_{\mathbf{T}}(z)$ is a complete unitary invariant for a pure Szegő tuple \mathbf{T} of Beurling type. This talk is based on a joint work with Prof. Jaydeb Sarkar and Dr. Ramlal Debnath.

Boyd indices and the complete story of the Berger-Coburn phenomenon

Jingbo Xia(夏经博)

University of Buffalo, USA

For a symmetrically normed ideal \mathcal{C}_{Φ} , its Boyd indices p_{Φ} and q_{Φ} are wellunderstood scalar

invariants, and they always satisfy the inequality $1 \leq p_\Phi \leq q_\Phi \leq \infty$. We settle the issue of Berger-Coburn phenomenon on the Fock space completely for general symmetrically normed ideals \mathcal{C}_Φ , where $\|\cdot\|_\Phi$ is not equivalent to the operator norm $\|\cdot\|$. We show that if the Boyd indices of \mathcal{C}_Φ satisfy the condition $1 < p_\Phi \leq q_\Phi < \infty$, then for $f \in L^\infty(\mathbb{C}^n)$, we have $H_f \in \mathcal{C}_\Phi$ if and only if $H_{\bar{f}} \in \mathcal{C}_\Phi$. We further show that if either $p_\Phi = 1$ or $q_\Phi = \infty$, then there is an $f \in L^\infty(\mathbb{C}^n)$ such that $H_f \in \mathcal{C}_\Phi$ while $H_{\bar{f}} \notin \mathcal{C}_\Phi$.

A joint spectral radius for tuples of operators

Orr Shalit

Technion - Israel Institute of Technology, Israel

The study of algebras of bounded noncommutative analytic functions on subvarieties of noncommutative unit balls has led us to associate a spectral radius function ρ_E with every finite-dimensional operator space E . Concretely, if $A = (A_1, \dots, A_d)$ is a d -tuple of operators, then $\rho_E(A)$ is defined via a certain tensor power limit formula, which reduces to Gelfand's spectral radius formula when E is one-dimensional. When E is the row operator space, ρ_E coincides with the joint spectral radius studied by Bunce, Popescu and others.

In a recent paper with Eli Shamovich, we introduced the joint spectral radius ρ_E and proved that $\rho_E(A) < 1$ if and only if A is jointly similar to a tuple that lies in the noncommutative ball corresponding to E . For example, when E is the row operator space, $\rho_E(A) < 1$ means that A is jointly similar to a strict row contraction. In this talk, based on joint work with Eli Shamovich, I will explain why we were led to this notion, present some examples, and describe possible applications. Finally, I will discuss recent progress on the case of commuting tuples, where several alternative notions of joint spectrum coincide.

Helton-Howe trace formulae on quotient modules

Lijia Ding (丁立家)

Zhengzhou University, China

In this talk, we will discuss Helton-Howe trace formulae on Hilbert modules over Stein strongly pseudoconvex finite manifolds. For higher-dimensional smooth subvarieties that transversely intersect with the strongly pseudoconvex boundary, we establish an integral trace formula for the compression of Toeplitz operators on holomorphic Sobolev quotient modules, provided the restriction maps satisfy a q -essentially isometric condition for some q strictly less than the dimension of the subvariety. Our findings extend known results from the unit ball to the Stein strongly pseudoconvex manifolds and partially answer a problem recently proposed for the Helton-Howe trace formula on quotient modules. This talk is based on a joint work with Prof. Kunyu Guo and Prof. Kai Wang.

Extension of contractive projections

Xiangdi Fu(付祥迪)

Hangzhou Institute for Advanced Study, UCAS, China

Through the establishment of several extension theorems, we provide explicit expressions for all contractive projections and 1 -complemented subspaces in the Hardy space $H^p(\mathbb{T})$ for $1 \leq p < \infty, p \neq 2$. Our characterization leads to two corollaries: first, all nontrivial 1 -complemented subspaces of $H^p(\mathbb{T})$ are isometric to $H^p(\mathbb{T})$; second, all contractive projections on $H^p(\mathbb{T})$ are restrictions of contractive projections on $L^p(\mathbb{T})$ that leave $H^p(\mathbb{T})$ invariant. The first corollary provides examples of prime Banach spaces in the isometric sense, while the second answers a question posed by P. Wojtaszczyk in 2003. This talk is based on a joint work (arXiv:2412.14808) with Professor Kunyu Guo and Dr. Dilong Li.

Some Clark Theory on the Bidisk

Kelly Bickel

Bucknell University, USA

Classical Clark measures are singular measures on the unit circle defined via inner functions that are closely tied to important topics in operator theory and complex analysis (for example, model spaces, compressed shifts, and composition operators). In this talk, we'll consider an analogous definition for Clark measures associated with twovariable inner functions. In the rational case, we'll give exact formulas for these Clark measures and characterize when associated Clark embeddings are unitary. For certain classes of two-variable model spaces, we will also use this theory to obtain nice unitary

Some results on analytic function spaces by potentials

Guanlong Bao(鲍官龙)

Shantou University, China

We talk about some results on analytic function spaces in terms of Newtonian potentials and certain variants of the Green potential. These results are about the problems of determining Carleson measures for the Bloch space and characterizing zero sets for Dirichlet spaces with harmonic weights.

Dynamical Frames and Hyperinvariant Subspaces

Victor Bailey

University of Oklahoma, USA

The theory of dynamical frames arose from practical problems in dynamical sampling where the initial state of a vector needs to be recovered from the space-time samples of future states of the vector. This leads to the investigation of structured frames obtained from the orbits of evolution operators. One of the basic problems in dynamical frame theory is to determine the semigroup representations, which we will call central frame representations, whose frame generators are unique (up to equivalence). In this talk, we will address the general uniqueness problem by presenting a characterization of central frame representations for any semigroup in terms of the co-hyperinvariant subspaces of the left regular representation of the semigroup. This result is not only consistent with the known result of Han and Larson in 2000 for group representation frames, but also proves that the frame vectors for any system of the form $\{A_1^{n_1} \cdots A_k^{n_k} : n_j \geq 0\}$, where $A_1, \dots, A_k \in B(H)$ commute, are equivalent. This is joint work with Deguang Han, Keri Kornelson, David Larson, and Rui Liu.

Subnormality of Brownian-type operators

Sameer Chavan

IIT Kanpur, India

In this talk, we discuss operators that are represented by upper triangular 2×2 block matrices whose entries satisfy some algebraic constraints. We call them Browniantype operators. These operators emerged from the study of Brownian isometries studied by Agler and Stankus via detailed analysis of the time shift operator of the modified Brownian motion process. We address the issue of subnormality of Brownian-type operators and relate it to a spectral inclusion of a pair of commuting normal operators.

This talk is based on a joint work with Z. J. Jabłoński, I. B. Jung and J. Stochel.

Measures on General Co-dimensional Surfaces in Innite Dimensions and Stokes Type Theorems

Jiayang Yu(余佳洋)

Sichuan University

In this talk, we construct explicitly measures on general co-dimensional surfaces in ℓ^2 which is, in some sense, the simplest infinite-dimensional space, closest to Euclidean spaces, but the construction of related surface measures is a longstanding unsolved problem. Our surface measures are naturally induced from the usual Gaussian measures on ℓ^2 , based on which we introduce the notion of differential forms and establish the corresponding Stokes type theorems.

Constrained sphere packing and the interpolation problem for positive definite functions

James Eldred Pascoe
Drexel University, USA

Delsarte's method provides a framework for analysis of sphere packing problems in terms of positive definite functions. Constrained packing, where only a prespecified set of angles between points may occur, is, in turn, naturally governed by the interpolation theory for positive definite functions. In this talk, we discuss the general theory of positive definite functions on the sphere, Delsarte's method and its geometric kernel embedding interpretation, related interpolation problems, and other topics. Based on joining work with Sujit Sakharam Damase.

Essential normality of quotient modules vs Hilbert-Schmidtness of submodules in Hardy modules over the polydisc

Penghui Wang(王鹏辉)
Shandong University, China

In this talk, I will introduce the recent development on the essential normality of quotient midules. Also, we will consider the relationship between the quotient modules with the Hilbert-Schmidtness of submodules. We find that all the finitely generated submodules containing a nonzero polynomial are Hilbert-Schmidt. The talk is based on the joint works with K.Guo, C.Zhao and Z.Zhu.

Brown-Halmos Characterization, and Function Theory on the Tetrablock

Paramita Pramanick
ISI Kolkata, India

We begin by establishing a Brown-Halmos type characterization of Toeplitz operators on the Hardy space associated with the tetrablock and as an application, we show that the zero operator is the only compact Toeplitz operator. Then we introduce a Schur-Agler type class associated with the tetrablock and establish a realization theorem for this class. Furthermore, we discuss a tetrablock analog of the interpolation theorem, extension theorem, and the Toeplitz corona theorem. true.

Singular Spectrum under a Wide Class of Perturbations

Constanze Liaw
University of Delaware, USA

For bounded self-adjoint operators A and K on a separable Hilbert space and a real parameter t

consider perturbed operators of the form $A + tK$. We present restrictions on the singular spectrum under trace class and more general perturbations as t is varied. To the best of our knowledge, these are the first statements on the singular spectrum under infinite rank perturbations and this work constitutes the first significant departure from the classical perturbation theory in half a century. This is joint work with Eero Saksman and Sergei Treil.

Hilbert-Schmidt norm estimates of homogeneous polynomial submodules in Hardy space over the bidisk

Chao Zu(组超)

Dalian University of Technology

In this talk, we will give a negative answer to the Hilbert-Schmidt norm boundedness problem for rank one polynomial submodules in Hardy space over the bidisk. For the homogeneous polynomial submodules $[(z - w)^k]$, by using the results about Toeplitz determinants with certain Fisher-Hartwig symbols, we show that the corresponding core operator C has eigenvalues $0, 1, \pm \frac{k}{n+k}, n \geq 1$. It implies that $2k - 1 < \|C\|_{\text{H.S.}}^2 < 2k + 1$, which tends to infinity when k tends to infinity. Moreover, we find that there is a close connection between the Hilbert-Schmidt norm estimates for homogeneous polynomial submodules and the Fisher-Hartwig conjecture, which describes the asymptotic behavior of Toeplitz determinants for a class of functions.

The complete Nevanlinna-Pick property for sub-Hardy/Bergman space

Yixin Yang(杨义新)

Dalian University of Technology

The complete Nevanlinna-Pick property(CNP) of a reproducing kernel Hilbert space is related to the solution of Nevanlinna-Pick interpolation problems, and has been studied extensively in the literature. One of the fundamental problem is to characterize for which reproducing kernel Hilbert spaces have the CNP? We will talk about the CNP of the sub-Hardy/Bergman space on polydisk, and see that when the kernel k tensor product or Schur product with an additional factor, the CNP will diminish. This is based on the joint work with Jiming Shen.



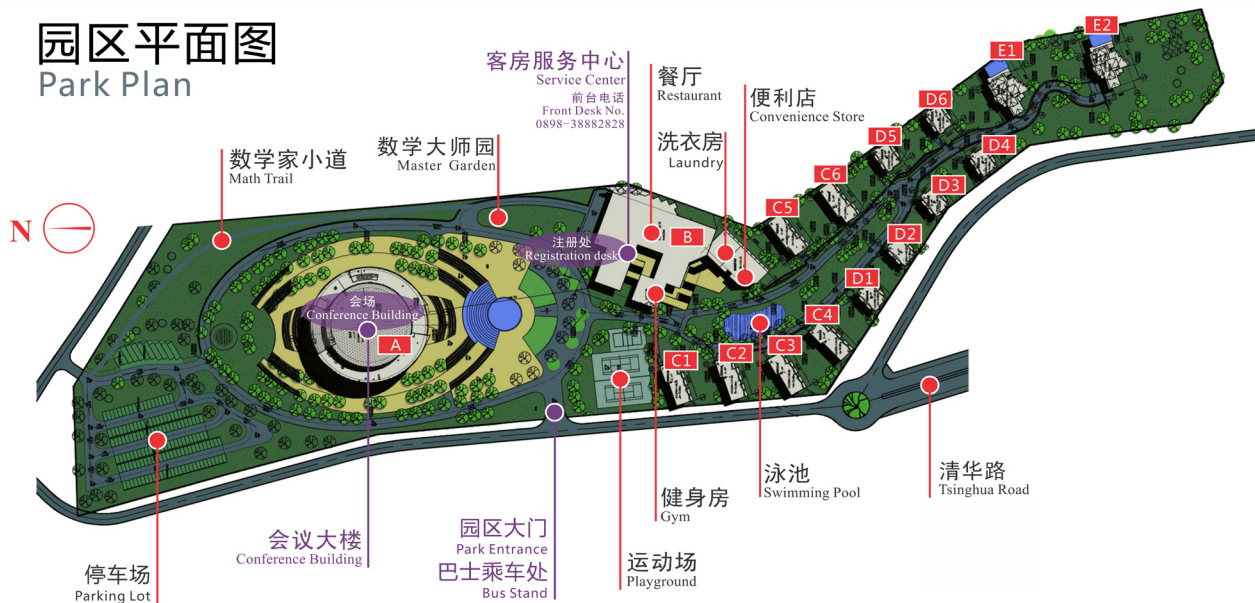
Welcome to TSIMF



The facilities of TSIMF are built on a 23-acre land surrounded by pristine environment at Phoenix Hill of Phoenix Township. The total square footage of all the facilities is over 29,000 square meter that includes state-of-the-art conference facilities (over 10,000 square meter) to hold many international workshops simultaneously, two reading rooms of library, a guest house (over 10,000 square meter) and the associated catering facilities, a large swimming pool, gym and sports court and other recreational facilities.

Management Center of Tsinghua Sanya International Forum is responsible for the construction, operation, management and service of TSIMF. The mission of TSIMF is to become a base for scientific innovations, and for nurturing of innovative human resource; through the interaction between leading mathematicians and core research groups in pure mathematics, applied mathematics, statistics, theoretical physics, applied physics, theoretical biology and other relating disciplines, TSIMF will provide a platform for exploring new directions, developing new methods, nurturing mathematical talents, and working to raise the level of mathematical research in China.

About Facilities



Registration

Conference booklets, room keys and name badges for all participants will be distributed at the front desk. Please take good care of your name badge. It is also your meal card and entrance ticket for all events.



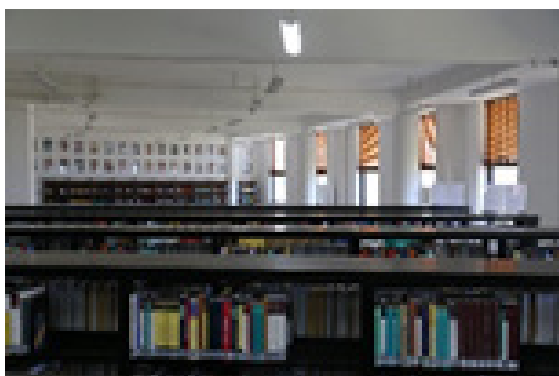
Guest Room

All the rooms are equipped with: free Wi-Fi (Password:tsimf123), TV, air conditioning and other utilities.

Family rooms are also equipped with kitchen and refrigerator.

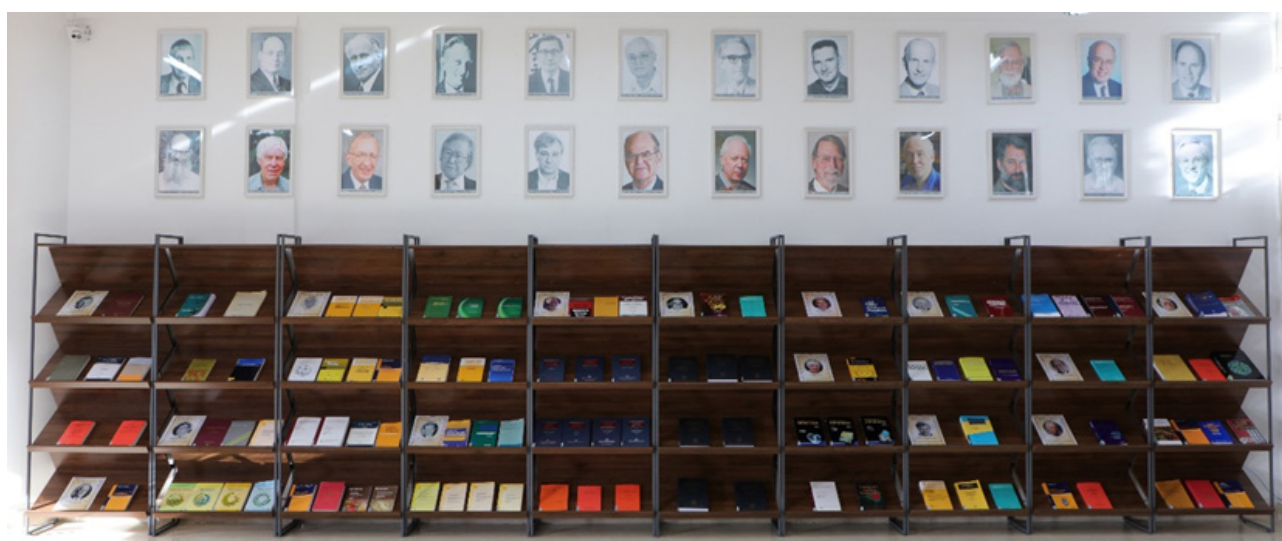


Library



Opening Hours: 09:00am-22:00pm

TSIMF library is available during the conference and can be accessed by using your room card. There is no need to sign out books but we ask that you kindly return any borrowed books to the book cart in library before your departure.



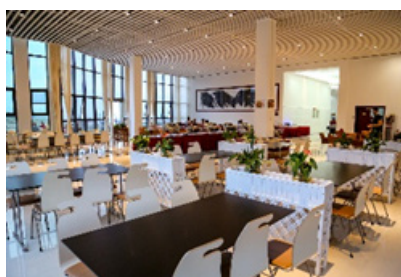
In order to give readers a better understanding of the contributions made by the Fields Medalists, the library of Tsinghua Sanya International Mathematics Forum (TSIMF) instituted the Special Collection of Fields Medalists as permanent collection of the library to serve the mathematical researchers and readers.

So far, there are 271 books from 49 authors in the Special Collection of Fields Medalists of TSIMF library. They are on display in room A220. The participants are welcome to visit.



Restaurant

All the meals are provided in the restaurant (Building B1) according to the time schedule.



Breakfast 07:30-08:30

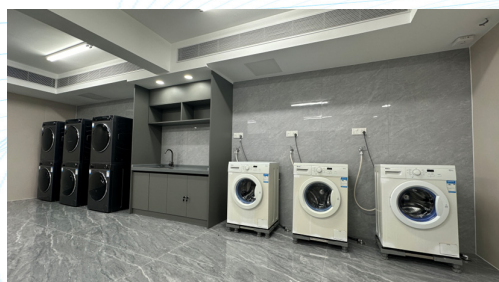
Lunch 12:00-13:30

Dinner 17:30-19:00

Laundry

Opening Hours: 24 hours

The self-service laundry room is located in the Building(B1).



Gym

Opening Hours: 24 hours

The gym is located in the Building 1 (B1), opposite to the reception hall. The gym provides various fitness equipment, as well as pool tables, tennis tables etc.



Playground

Playground is located on the east of the central gate. There you can play basketball, tennis and badminton. Meanwhile, you can borrow table tennis, basketball, tennis balls and badminton at the reception desk.

Swimming Pool

Please enter the pool during the open hours, swimming attire and swim caps are required, if you feel unwell while swimming, please stop swimming immediately and get out of the pool. The depth of the pool is 1.2M-1.8M.

Opening Hours: 13:00-14:00 18:00-21:00



Free Shuttle Bus Service at TSIMF

We provide free shuttle bus for participants and you are always welcome to take our shuttle bus, all you need to do is wave your hands to stop the bus.

Destinations: Conference Building, Reception Room, Restaurant, Swimming Pool, Hotel etc.



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